

Декартовы координаты. Пространственная траектория

Точка движется по закону $x = x(t), y = y(t), z = z(t)$. Определить скорость, ускорение точки и радиус кривизны траектории при $t = t_1$ (x, y и z даны в см, t и t_1 — в с).

Кирсанов М.Н. **Решебник. Теоретическая механика**/Под ред. А. И. Кириллова.— М.:ФИЗМАТЛИТ, 2002.— 384 с. (с.137.)

Задача 2.1.

$$\begin{aligned}x &= 7\sqrt{2t+7}, \\y &= \frac{1}{2}\sin^2 8t - 7t, \\z &= 3t^2 + 7t + 2, \quad t_1 = 0.6.\end{aligned}$$

Задача 2.2.

$$\begin{aligned}x &= 10(t+1)^{1/10}, \\y &= 10t + \frac{1}{4}\cos^2 8t, \\z &= \frac{12}{t+2}, \quad t_1 = 0.8.\end{aligned}$$

Задача 2.3.

$$\begin{aligned}x &= 2e^{(t^2)}, \\y &= t^2 + 2t + 4, \\z &= \ln(4t+2), \quad t_1 = 0.1.\end{aligned}$$

Задача 2.4.

$$\begin{aligned}x &= 11\sqrt{4t+11}, \\y &= 12t + \frac{1}{4}\cos^2 8t, \\z &= 3\operatorname{tg}(t/2), \quad t_1 = 1.\end{aligned}$$

Задача 2.5.

$$\begin{aligned}x &= 2t^2 + 11t + 3, \\y &= 3\arcsin(t/11), \\z &= 11e^{(t^2)}, \quad t_1 = 1.\end{aligned}$$

Задача 2.6.

$$\begin{aligned}x &= 6(t+1)^{1/5}, \\y &= 4\ln(3t+2), \\z &= 2t^2 + 5t + 3, \quad t_1 = 0.4.\end{aligned}$$

Задача 2.7.

$$\begin{aligned}x &= 4t + \cos^2 4t, \\y &= 3\sqrt{2t+3}, \\z &= 13e^{t/4}, \quad t_1 = 0.2.\end{aligned}$$

Задача 2.8.

$$\begin{aligned}x &= 7\sqrt{3t+7}, \\y &= 7e^{(t^2)}, \\z &= 4\operatorname{tg}(t/3), \quad t_1 = 0.6.\end{aligned}$$

Задача 2.9.

$$\begin{aligned}x &= 5\ln(2t+2), \\y &= 6e^{(t^2)}, \\z &= 3t^2 + 6t + 2, \quad t_1 = 0.5.\end{aligned}$$

Задача 2.10.

$$\begin{aligned}x &= 3e^{(t^2)}, \\y &= \frac{1}{2}\sin 6t + 3t, \\z &= 3\arcsin(t/3), \quad t_1 = 0.2.\end{aligned}$$

Задача 2.11.

$$\begin{aligned}x &= 7\sqrt{2t+7}, \\y &= \frac{1}{2}\sin^2 8t - 7t, \\z &= 8(t+1)^{3/10}, \quad t_1 = 0.6.\end{aligned}$$

Задача 2.12.

$$\begin{aligned}x &= 8(t+1)^{3/10}, \\y &= \frac{10}{3t+4}, \\z &= \frac{1}{2}\sin 8t + 7t, \quad t_1 = 0.6.\end{aligned}$$

Задача 2.13.

$$\begin{aligned}x &= 13e^{t/3}, \\y &= \frac{1}{2}\sin^2 6t - 3t, \\z &= \frac{1}{2}\sin 6t + 3t, \quad t_1 = 0.2.\end{aligned}$$

Задача 2.14.

$$\begin{aligned}x &= 2\arcsin(t/6), \\y &= \frac{1}{2}\sin 4t + 6t, \\z &= 3\operatorname{tg}(t/2), \quad t_1 = 0.5.\end{aligned}$$

Задача 2.15.

$$\begin{aligned}x &= 3t^2 + 3t + 2, \\y &= 4(t+1)^{3/10}, \\z &= \frac{1}{2}\sin 8t + 3t, \quad t_1 = 0.2.\end{aligned}$$

Задача 2.16.

6

$$\begin{aligned}x &= 13e^{t/2}, \\y &= 2 \ln(4t + 2), \\z &= t^2 + 3t + 4, \quad t_1 = 0.2.\end{aligned}$$

Задача 2.17.

6

$$\begin{aligned}x &= 2\sqrt{3t + 2}, \\y &= 3t + \frac{1}{2} \cos^2 6t, \\z &= \frac{1}{2} \sin^2 6t - 2t, \quad t_1 = 0.1.\end{aligned}$$

Задача 2.18.

6

$$\begin{aligned}x &= 8e^{(t^2)}, \\y &= \frac{11}{3t + 4}, \\z &= \frac{1}{2} \sin 8t + 8t, \quad t_1 = 0.7.\end{aligned}$$

Задача 2.19.

6

$$\begin{aligned}x &= \frac{11}{2t + 3}, \\y &= 7 \ln(3t + 2), \\z &= 18e^{t/3}, \quad t_1 = 0.7.\end{aligned}$$

Задача 2.20.

6

$$\begin{aligned}x &= 2\arcsin(t/7), \\y &= t^2 + 7t + 4, \\z &= 7e^{(t^2)}, \quad t_1 = 0.6.\end{aligned}$$

Задача 2.21.

6

$$\begin{aligned}x &= 3t + \cos^2 4t, \\y &= \frac{1}{2} \sin 8t + 2t, \\z &= 5\operatorname{tg}(t/4), \quad t_1 = 0.1.\end{aligned}$$

Задача 2.22.

6

$$\begin{aligned}x &= 6(t + 1)^{1/10}, \\y &= \frac{8}{t + 2}, \\z &= 6t + \frac{1}{4} \cos^2 8t, \quad t_1 = 0.4.\end{aligned}$$

Задача 2.23.

6

$$\begin{aligned}x &= 5\sqrt{3t + 5}, \\y &= \frac{1}{2} \sin 6t + 5t, \\z &= 6(t + 1)^{1/5}, \quad t_1 = 0.4.\end{aligned}$$

Задача 2.24.

6

$$\begin{aligned}x &= t^2 + 2t + 4, \\y &= \frac{5}{t + 2}, \\z &= 2\sqrt{4t + 2}, \quad t_1 = 0.1.\end{aligned}$$

Задача 2.25.

6

$$\begin{aligned}x &= \frac{1}{2} \sin^2 6t - 7t, \\y &= 2t^2 + 7t + 3, \\z &= 8(t + 1)^{1/5}, \quad t_1 = 0.6.\end{aligned}$$

Задача 2.26.

6

$$\begin{aligned}x &= \frac{1}{2} \sin 6t + 4t, \\y &= \frac{7}{2t + 3}, \\z &= 3\arcsin(t/4), \quad t_1 = 0.3.\end{aligned}$$

Задача 2.27.

6

$$\begin{aligned}x &= 3(t + 1)^{1/10}, \\y &= \ln(4t + 2), \\z &= 12e^{t/2}, \quad t_1 = 0.1.\end{aligned}$$

Задача 2.28.

6

$$\begin{aligned}x &= t^2 + 9t + 4, \\y &= 19e^{t/2}, \\z &= 10(t + 1)^{1/10}, \quad t_1 = 0.8.\end{aligned}$$

Задача 2.29.

6

$$\begin{aligned}x &= 4\sqrt{2t + 4}, \\y &= 14e^{t/4}, \\z &= 5(t + 1)^{3/10}, \quad t_1 = 0.3.\end{aligned}$$

Задача 2.30.

6

$$\begin{aligned}x &= 8t + \frac{1}{2} \cos^2 6t, \\y &= 17e^{t/3}, \\z &= \frac{1}{2} \sin^2 6t - 7t, \quad t_1 = 0.6.\end{aligned}$$

Задача 2.31.

6

$$\begin{aligned}x &= \frac{1}{2} \sin^2 6t - 2t, \\y &= 2\sqrt{3t + 2}, \\z &= 3t + \frac{1}{2} \cos^2 6t, \quad t_1 = 0.1.\end{aligned}$$

Задача 2.32.

6

$$\begin{aligned}x &= 5(t + 1)^{1/5}, \\y &= \frac{1}{2} \sin 6t + 4t, \\z &= \frac{1}{2} \sin^2 6t - 4t, \quad t_1 = 0.3.\end{aligned}$$

Задача 2.33.

6

$$\begin{aligned}x &= 3\operatorname{tg}(t/2), \\y &= \frac{10}{t + 2}, \\z &= 8t + \frac{1}{4} \cos^2 8t, \quad t_1 = 0.6.\end{aligned}$$

Декартовы координаты. Пространственная траектория

№	v_x	v_y	v_z	v	a_x	a_y	a_z	a	a_τ	a_n	R
1	2.44	-7.70	10.60	13.33	-0.30	-63.02	6.00	63.31	41.12	48.13	3.689
2	0.59	9.54	-1.53	9.68	-0.29	-31.13	1.09	31.15	-30.87	4.17	22.467
3	0.40	2.20	1.67	2.79	4.12	2.00	-2.78	5.36	0.51	5.33	1.459
4	5.68	12.58	1.95	13.94	-0.76	30.65	1.06	30.67	27.49	13.60	14.282
5	15.00	0.27	59.80	61.66	4.00	0.00	179.41	179.45	174.99	39.78	95.570
6	0.92	3.75	6.60	7.65	-0.52	-3.52	4.00	5.35	1.67	5.09	11.497
7	0.00	1.63	3.42	3.78	0.93	-0.48	0.85	1.35	0.57	1.23	11.648
8	3.54	12.04	1.39	12.63	-0.60	34.51	0.19	34.52	32.76	10.87	14.665
9	3.33	7.70	9.00	12.31	-2.22	23.11	6.00	23.98	18.25	15.55	9.738
10	1.25	4.09	1.00	4.39	6.74	-16.78	0.02	18.08	-13.70	11.80	1.632
11	2.44	-7.70	1.73	8.26	-0.30	-63.02	-0.76	63.03	58.49	23.48	2.905
12	1.73	-0.89	7.35	7.60	-0.76	0.92	31.88	31.90	30.54	9.22	6.269
13	4.63	-0.97	4.09	6.25	1.54	-26.55	-16.78	31.44	-5.69	30.92	1.265
14	0.33	5.17	1.60	5.42	0.00	-7.27	0.41	7.29	-6.82	2.57	11.410
15	4.20	1.06	2.88	5.20	6.00	-0.62	-31.99	32.55	-13.01	29.84	0.907
16	7.18	2.86	3.40	8.45	3.59	-4.08	2.00	5.79	2.48	5.24	13.623
17	1.98	0.20	0.80	2.14	-1.29	-13.04	13.04	18.49	2.42	18.33	0.250
18	18.28	-0.89	11.10	21.41	51.71	0.87	20.20	55.52	54.60	10.08	45.480
19	-1.14	5.12	7.58	9.22	1.03	-3.75	2.53	4.64	-0.13	4.63	18.328
20	0.29	8.20	12.04	14.57	0.00	2.00	34.51	34.57	29.65	17.79	11.936
21	0.13	4.79	1.25	4.95	-22.29	-22.96	0.02	32.00	-22.79	22.47	1.090
22	0.44	-1.39	5.77	5.95	-0.28	1.16	-31.78	31.80	-31.10	6.64	5.331
23	3.01	2.79	0.92	4.21	-0.73	-12.16	-0.52	12.19	-8.70	8.54	2.070
24	2.20	-1.13	2.58	3.58	2.00	1.08	-2.15	3.13	-0.67	3.06	4.183
25	-4.62	9.40	1.10	10.53	21.90	4.00	-0.55	22.27	-6.09	21.42	5.177
26	3.32	-1.08	0.75	3.57	-17.53	1.20	0.01	17.57	-16.65	5.60	2.276
27	0.28	1.67	6.31	6.53	-0.23	-2.78	3.15	4.21	2.33	3.51	12.161
28	10.60	14.17	0.59	17.71	2.00	7.09	-0.29	7.37	6.86	2.69	116.398
29	1.87	3.77	1.25	4.39	-0.41	0.94	-0.67	1.23	0.45	1.14	16.863
30	5.62	6.92	-4.62	10.04	-21.90	2.31	21.90	31.06	-20.74	23.12	4.361
31	0.80	1.98	0.20	2.14	13.04	-1.29	-13.04	18.49	2.42	18.33	0.250
32	0.81	3.32	-5.33	6.33	-0.50	-17.53	-32.28	36.74	17.92	32.07	1.249
33	1.64	-1.48	8.35	8.64	0.51	1.14	31.51	31.53	30.36	8.52	8.754