

Декартовы координаты. Пространственная траектория

Точка движется по закону $x = x(t), y = y(t), z = z(t)$. Определить скорость, ускорение точки и радиус кривизны траектории при $t = t_1$ (x, y и z даны в см, t и t_1 — в с).

Кирсанов М.Н. **Решebник. Теоретическая механика**/Под ред. А. И. Кириллова.— М.:ФИЗМАТЛИТ, 2002.— 384 с. (с.137.)

Задача 2.1.

$$\begin{aligned}x &= 2\arcsin(t/7), \\y &= 6 \ln(4t + 2), \\z &= \frac{1}{2} \sin 4t + 7t, \quad t_1 = 0.6.\end{aligned}$$

Задача 2.2.

$$\begin{aligned}x &= 4\arcsin(t/8), \\y &= \frac{11}{3t + 4}, \\z &= \frac{1}{2} \sin^2 8t - 8t, \quad t_1 = 0.7.\end{aligned}$$

Задача 2.3.

$$\begin{aligned}x &= 9\sqrt{3t + 9}, \\y &= \frac{1}{2} \sin 6t + 9t, \\z &= 2t^2 + 9t + 3, \quad t_1 = 0.8.\end{aligned}$$

Задача 2.4.

$$\begin{aligned}x &= 5e^{(t^2)}, \\y &= 3\arcsin(t/5), \\z &= 4\operatorname{tg}(t/3), \quad t_1 = 0.4.\end{aligned}$$

Задача 2.5.

$$\begin{aligned}x &= 4(t + 1)^{3/10}, \\y &= 3t^2 + 3t + 2, \\z &= \frac{6}{3t + 4}, \quad t_1 = 0.2.\end{aligned}$$

Задача 2.6.

$$\begin{aligned}x &= 2t^2 + 8t + 3, \\y &= 9t + \frac{1}{2} \cos^2 6t, \\z &= \frac{1}{2} \sin^2 6t - 8t, \quad t_1 = 0.7.\end{aligned}$$

Задача 2.7.

$$\begin{aligned}x &= 3t + \frac{1}{2} \cos^2 6t, \\y &= 2\sqrt{3t + 2}, \\z &= 3\arcsin(t/2), \quad t_1 = 0.1.\end{aligned}$$

Задача 2.8.

$$\begin{aligned}x &= 9(t + 1)^{1/5}, \\y &= 9t + \frac{1}{2} \cos^2 6t, \\z &= 18e^{t/3}, \quad t_1 = 0.7.\end{aligned}$$

Задача 2.9.

$$\begin{aligned}x &= \frac{1}{2} \sin^2 4t - 7t, \\y &= \frac{1}{2} \sin 4t + 7t, \\z &= 6 \ln(4t + 2), \quad t_1 = 0.6.\end{aligned}$$

Задача 2.10.

$$\begin{aligned}x &= 6 \ln(4t + 2), \\y &= \frac{1}{2} \sin 4t + 7t, \\z &= t^2 + 7t + 4, \quad t_1 = 0.6.\end{aligned}$$

Задача 2.11.

$$\begin{aligned}x &= \frac{1}{2} \sin^2 4t - 2t, \\y &= 12e^{t/2}, \\z &= 3(t + 1)^{1/10}, \quad t_1 = 0.1.\end{aligned}$$

Задача 2.12.

$$\begin{aligned}x &= 19e^{t/4}, \\y &= 5\operatorname{tg}(t/4), \\z &= 8 \ln(2t + 2), \quad t_1 = 0.8.\end{aligned}$$

Задача 2.13.

$$\begin{aligned}x &= \frac{1}{2} \sin 4t + 5t, \\y &= 5e^{(t^2)}, \\z &= 2\arcsin(t/5), \quad t_1 = 0.4.\end{aligned}$$

Задача 2.14.

$$\begin{aligned}x &= 18e^{t/2}, \\y &= 8e^{(t^2)}, \\z &= 2\arcsin(t/8), \quad t_1 = 0.7.\end{aligned}$$

Задача 2.15.

$$\begin{aligned}x &= 2\arcsin(t/6), \\y &= \frac{9}{t + 2}, \\z &= \frac{1}{2} \sin 4t + 6t, \quad t_1 = 0.5.\end{aligned}$$

Задача 2.16.

7

$$\begin{aligned}x &= 5e^{(t^2)}, \\y &= \frac{1}{2} \sin^2 4t - 5t, \\z &= 5\sqrt{4t+5}, \quad t_1 = 0.4.\end{aligned}$$

Задача 2.17.

7

$$\begin{aligned}x &= 8e^{(t^2)}, \\y &= 7 \ln(2t+2), \\z &= 8\sqrt{2t+8}, \quad t_1 = 0.7.\end{aligned}$$

Задача 2.18.

7

$$\begin{aligned}x &= \frac{7}{2t+3}, \\y &= 5(t+1)^{1/5}, \\z &= 4\operatorname{tg}(t/3), \quad t_1 = 0.3.\end{aligned}$$

Задача 2.19.

7

$$\begin{aligned}x &= \frac{9}{t+2}, \\y &= t^2 + 6t + 4, \\z &= 5 \ln(4t+2), \quad t_1 = 0.5.\end{aligned}$$

Задача 2.20.

7

$$\begin{aligned}x &= 18e^{t/4}, \\y &= \frac{1}{2} \sin^2 8t - 8t, \\z &= 8e^{(t^2)}, \quad t_1 = 0.7.\end{aligned}$$

Задача 2.21.

7

$$\begin{aligned}x &= t^2 + 6t + 4, \\y &= 2\arcsin(t/6), \\z &= 6e^{(t^2)}, \quad t_1 = 0.5.\end{aligned}$$

Задача 2.22.

7

$$\begin{aligned}x &= 7e^{(t^2)}, \\y &= 2\arcsin(t/7), \\z &= 7\sqrt{4t+7}, \quad t_1 = 0.6.\end{aligned}$$

Задача 2.23.

7

$$\begin{aligned}x &= 9t + \frac{1}{4} \cos^2 8t, \\y &= 2\arcsin(t/8), \\z &= 8\sqrt{4t+8}, \quad t_1 = 0.7.\end{aligned}$$

Задача 2.24.

7

$$\begin{aligned}x &= 3\operatorname{tg}(t/2), \\y &= t^2 + 3t + 4, \\z &= 2 \ln(4t+2), \quad t_1 = 0.2.\end{aligned}$$

Задача 2.25.

7

$$\begin{aligned}x &= \frac{6}{2t+3}, \\y &= 4\operatorname{tg}(t/3), \\z &= 2 \ln(3t+2), \quad t_1 = 0.2.\end{aligned}$$

Задача 2.26.

7

$$\begin{aligned}x &= 8(t+1)^{1/10}, \\y &= 7e^{(t^2)}, \\z &= 2\arcsin(t/7), \quad t_1 = 0.6.\end{aligned}$$

Задача 2.27.

7

$$\begin{aligned}x &= 3\arcsin(t/11), \\y &= 21e^{t/3}, \\z &= 12t + \frac{1}{2} \cos^2 6t, \quad t_1 = 1.\end{aligned}$$

Задача 2.28.

7

$$\begin{aligned}x &= \frac{1}{2} \sin 6t + 4t, \\y &= 14e^{t/3}, \\z &= 3 \ln(3t+2), \quad t_1 = 0.3.\end{aligned}$$

Задача 2.29.

7

$$\begin{aligned}x &= 2e^{(t^2)}, \\y &= 5\operatorname{tg}(t/4), \\z &= 2\sqrt{2t+2}, \quad t_1 = 0.1.\end{aligned}$$

Задача 2.30.

7

$$\begin{aligned}x &= 4\arcsin(t/11), \\y &= 11\sqrt{2t+11}, \\z &= \frac{1}{2} \sin^2 8t - 11t, \quad t_1 = 1.\end{aligned}$$

Задача 2.31.

7

$$\begin{aligned}x &= 10t + \frac{1}{2} \cos^2 6t, \\y &= 19e^{t/3}, \\z &= 9\sqrt{3t+9}, \quad t_1 = 0.8.\end{aligned}$$

Задача 2.32.

7

$$\begin{aligned}x &= 17e^{t/4}, \\y &= \frac{1}{2} \sin^2 8t - 7t, \\z &= 8(t+1)^{3/10}, \quad t_1 = 0.6.\end{aligned}$$

Задача 2.33.

7

$$\begin{aligned}x &= 5\operatorname{tg}(t/4), \\y &= \frac{1}{2} \sin 8t + 11t, \\z &= 3t^2 + 11t + 2, \quad t_1 = 1.\end{aligned}$$

Декартовы координаты. Пространственная траектория

№	v_x	v_y	v_z	v	a_x	a_y	a_z	a	a_τ	a_n	R
1	0.29	5.45	5.53	7.77	0.00	-4.96	-5.40	7.33	-7.32	0.38	157.612
2	0.50	-0.89	-11.92	11.96	0.01	0.87	12.99	13.02	-13.01	0.56	255.449
3	4.00	9.26	12.20	15.83	-0.53	17.93	4.00	18.38	13.44	12.54	19.993
4	4.69	0.60	1.36	4.92	15.49	0.01	0.12	15.49	14.80	4.56	5.313
5	1.06	4.20	-0.85	4.41	-0.62	6.00	1.11	6.13	5.35	3.00	6.491
6	10.80	6.44	-5.44	13.70	4.00	18.69	-18.69	26.74	19.36	18.45	10.171
7	0.20	1.98	1.50	2.49	-13.04	-1.29	0.04	13.11	-2.07	12.94	0.480
8	1.18	6.44	7.58	10.01	-0.55	18.69	2.53	18.87	13.87	12.80	7.828
9	-8.99	5.53	5.45	11.88	1.40	-5.40	-4.96	7.47	-5.85	4.64	30.416
10	5.45	5.53	8.20	11.29	-4.96	-5.40	2.00	7.60	-3.59	6.70	19.026
11	-0.57	6.31	0.28	6.34	11.15	3.15	-0.23	11.59	2.13	11.39	3.528
12	5.80	1.30	4.44	7.42	1.45	0.13	-2.47	2.87	-0.32	2.85	19.345
13	4.94	4.69	0.40	6.83	-8.00	15.49	0.01	17.43	4.86	16.74	2.784
14	12.77	18.28	0.25	22.30	6.39	51.71	0.00	52.10	46.05	24.39	20.398
15	0.33	-1.44	5.17	5.38	0.00	1.15	-7.27	7.37	-7.30	0.96	30.086
16	4.69	-5.12	3.89	7.96	15.49	-15.97	-1.18	22.28	18.82	11.92	5.316
17	18.28	4.12	2.61	18.92	51.71	-2.42	-0.28	51.77	49.40	15.48	23.126
18	-1.08	0.81	1.35	1.91	1.20	-0.50	0.09	1.30	-0.83	1.01	3.617
19	-1.44	7.00	5.00	8.72	1.15	2.00	-5.00	5.51	-1.45	5.31	14.320
20	5.36	-11.92	18.28	22.47	1.34	12.99	51.71	53.34	35.50	39.80	12.686
21	7.00	0.33	7.70	10.41	2.00	0.00	23.11	23.20	18.44	14.07	7.707
22	12.04	0.29	4.57	12.88	34.51	0.00	-0.97	34.53	31.92	13.17	12.599
23	10.96	0.25	4.87	11.99	-6.50	0.00	-0.90	6.56	-6.30	1.82	79.100
24	1.52	3.40	2.86	4.69	0.15	2.00	-4.08	4.55	-0.99	4.44	4.960
25	-1.04	1.34	2.31	2.86	1.22	0.06	-2.66	2.93	-2.56	1.42	5.759
26	0.52	12.04	0.29	12.05	-0.29	34.51	0.00	34.52	34.46	1.97	73.679
27	0.27	9.77	13.61	16.76	0.00	3.26	-30.38	30.55	-22.78	20.36	13.786
28	3.32	5.16	3.10	6.87	-17.53	1.72	-3.21	17.90	-8.62	15.69	3.011
29	0.40	1.25	1.35	1.88	4.12	0.02	-0.61	4.17	0.46	4.14	0.856
30	0.37	3.05	-12.15	12.53	0.00	-0.23	-61.29	61.29	59.36	15.25	10.302
31	10.52	8.27	4.00	13.97	35.45	2.76	-0.53	35.56	28.19	21.68	9.000
32	4.94	-7.70	1.73	9.31	1.23	-63.02	-0.76	63.04	52.64	34.68	2.497
33	1.33	10.42	17.00	19.98	0.17	-31.66	6.00	32.22	-11.39	30.14	13.247